## Exercise 15

For the following exercises, find the domain, range, and all zeros/intercepts, if any, of the functions.

$$
g(x)=\sqrt{8 x-1}
$$

## Solution

$g(x)$ is a square root function, so the domain is the set of all $x$ where the argument is nonnegative.

$$
\begin{aligned}
8 x-1 & \geq 0 \\
8 x & \geq 1 \\
x & \geq \frac{1}{8}
\end{aligned}
$$

Therefore, the domain is $\{x \mid x \geq 1 / 8\}$. The square root yields a nonnegative number for any value of $x$ in the domain, so the range is $\{y \mid 0 \leq y<\infty\}$. Find the zero now.

$$
g(x)=\sqrt{8 x-1}=0 \quad \Rightarrow \quad x=\frac{1}{8}
$$

The one $x$-intercept is $(1 / 8,0)$. Below is a graph of $g(x)$ versus $x$ to confirm these results.


